

# TCA UO<sub>2</sub> / MOX Core Analyses

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In order to examine the adequacy of nuclear data, the TCA UO<sub>2</sub> and MOX core experiments were analyzed with MVP using the libraries based on ENDF/B-VI Mod.3 and JENDL-3.2. The ENDF/B-VI data underpredict  $k_{\text{eff}}$  values. The replacement of <sup>238</sup>U data with the JENDL-3.2 data and the adjustment of <sup>235</sup>v-value raise the  $k_{\text{eff}}$  values by 0.3% for UO<sub>2</sub> cores, but still underpredict  $k_{\text{eff}}$  values. On the other hand, the nuclear data of JENDL-3.2 for H, O, Al, <sup>238</sup>U and <sup>235</sup>U of ENDF/B-VI whose <sup>235</sup>v-value in thermal energy region is adjusted to the average value of JENDL-3.2 give a good prediction of  $k_{\text{eff}}$ .

**1. Introduction** UO<sub>2</sub> and MOX core experiments carried out using TCA of JAERI have been analyzed with the continuous energy Monte Carlo code MVP using the libraries based on ENDF/B-VI Mod.3 and JENDL-3.2 to examine the adequacy of the nuclear data. The effect on  $k_{\text{eff}}$  with fuel burnup was also evaluated with 2-D transport depletion calculation code PHOENIX-P using a 70-group library based on ENDF/B-VI.

**2. Analyses and discussions** MVP calculations are performed in three-dimensional core configuration shown in Fig.1. The cores whose moderator to fuel volume ratios are 1.5 ~ 3.0 for UO<sub>2</sub> and 2.42 ~ 5.55 for MOX are analyzed. The three libraries are examined here : ENDF/B-VI; ENDF/B-VI whose <sup>238</sup>U data are replaced with that of JENDL3.2;

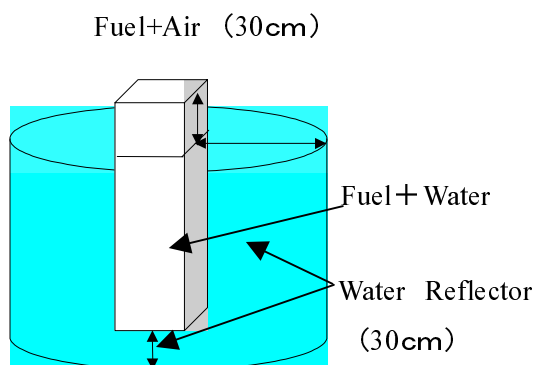


Fig.1 Core Configuration

JENDL3.2. The results are shown in Table-1.

The followings can be found from the table :

ENDF/B-VI gives lower  $k_{\text{eff}}$  by about 0.5%  $k/k$  for UO<sub>2</sub> cores and about 0.25%  $k/k$  for MOX cores,

<sup>238</sup>U of JENDL-3.2 raises  $k_{\text{eff}}$  by 0.2%  $k/k$  for UO<sub>2</sub> cores and 0.1%  $k/k$  for MOX cores,

JENDL3.2 gives higher  $k_{\text{eff}}$  by 0.2 to 0.4%  $k/k$  for UO<sub>2</sub> cores and 0.1 to 0.2%  $k/k$  for MOX cores.

Table-1  $k_{eff}$  calculated with MVP for TCA U/MOX Cores

Core Name	Fuel rods array	EN/B-VI*	EN/B-VI+ J3.2 $^{238}\text{U}$	JENDL3.2
1.50U	24X24	$0.99508 \pm 0.0251\%$	$0.99738 \pm 0.0243\%$	$1.00419 \pm 0.0232\%$
1.83U	22X22	$0.99448 \pm 0.0250\%$	$0.99661 \pm 0.0237\%$	$1.00290 \pm 0.0244\%$
2.48U	20X20	$0.99448 \pm 0.0245\%$	$0.99614 \pm 0.0240\%$	$1.00251 \pm 0.0243\%$
3.00U	19X19	$0.99444 \pm 0.0246\%$	$0.99658 \pm 0.0232\%$	$1.00206 \pm 0.0230\%$
2.42Pu	22X22	$0.99735 \pm 0.0236\%$	$0.99843 \pm 0.0235\%$	$1.00095 \pm 0.0240\%$
2.98Pu	21X21	$0.99782 \pm 0.0239\%$	$0.99882 \pm 0.0234\%$	$1.00197 \pm 0.0232\%$
4.24Pu	20X20	$0.99788 \pm 0.0232\%$	$0.99878 \pm 0.0229\%$	$1.00135 \pm 0.0224\%$
5.55Pu	21X21	$0.99729 \pm 0.0216\%$	$0.99825 \pm 0.0215\%$	$1.00187 \pm 0.0218\%$

\* A cross-section library based on the ENDF/B-VI Mod.3 is used

The results are also shown in Fig.2 and Fig.3.

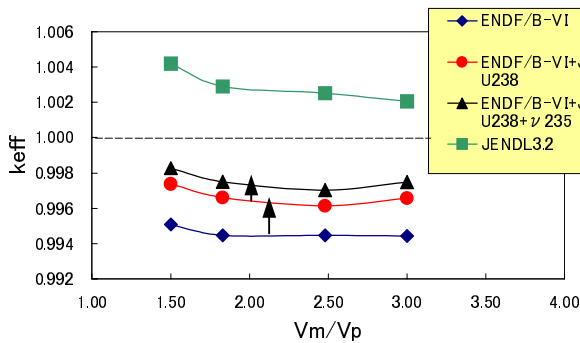


Fig.2 keff of TCA UO2 Core

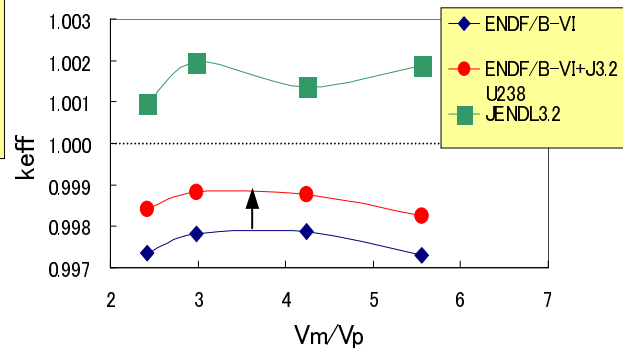


Fig.3 keff of TCA MOX Core

The reason why ENDF/B-VI data underpredict  $k_{eff}$  values was investigated. According to H.Takano, the  $k_{eff}$  values calculated with ENDF/B-VI are underpredicted and the harder neutron spectrum due to the inelastic scattering of  $^{238}\text{U}$  and the  $\nu$ -value of  $^{235}\text{U}$  are the cause of the underprediction[1]. Therefore, we did the check calculations to confirm the effects.

First, we processed inelastic cross-sections and scattering matrices of  $^{238}\text{U}$  of ENDF/B-VI and JENDL-3.2 with NJOY. The results are shown in Fig.4 and Fig.5.

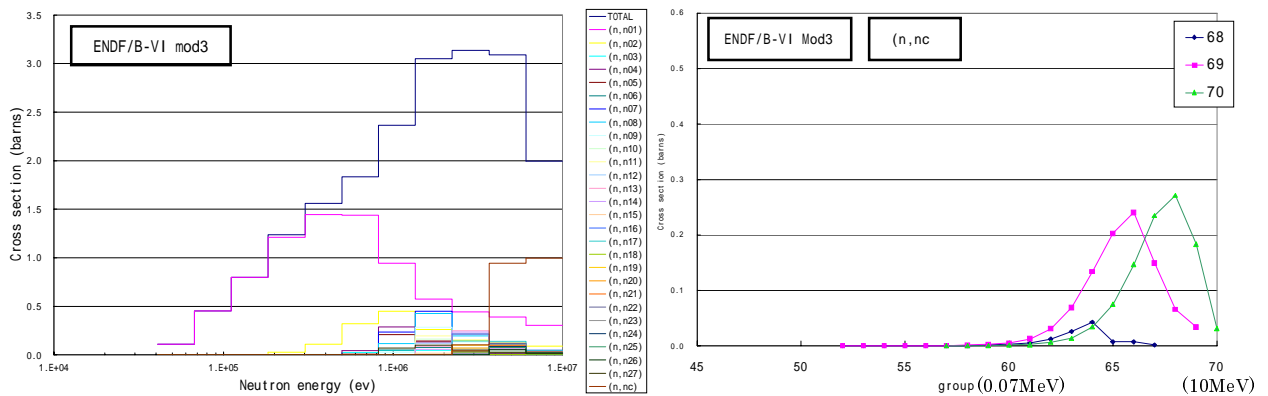


Fig.4 In-elastic Scattering Cross-sections and Matrix of ENDF/B-VI

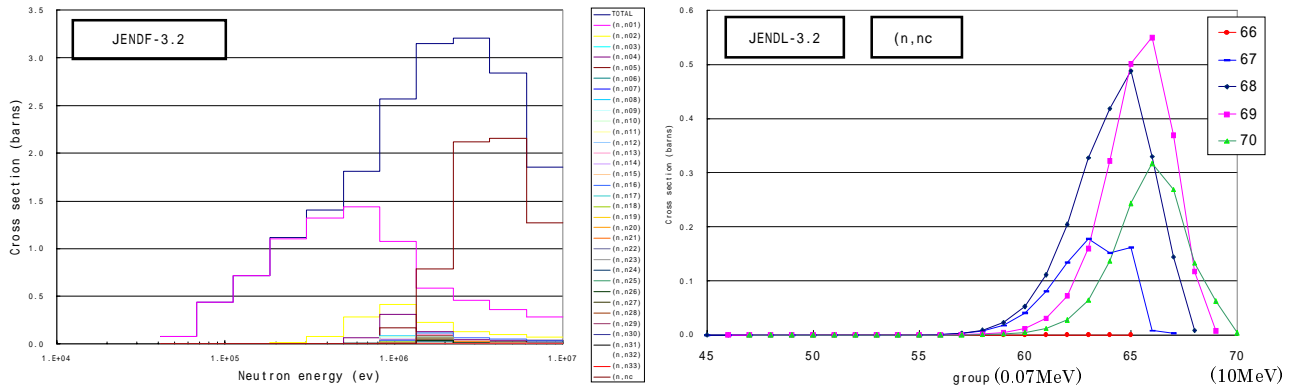


Fig.5 In-elastic Scattering Cross-sections and Matrix of JENDL-3.2

It is obvious from the figures that the continuum scattering matrix of ENDF/B-VI is smaller than that of JENDL-3.2 and gives harder neutron spectrum, and hence more neutron leakage.

In order to confirm that the cause of the underprediction of  $k_{eff}$  for the TCA critical experiments is the neutron leakage from the core, the  $k_{inf}$  values of MVP were compared for an infinite array of the PWR standard cell shown in Fig.6. As can be seen from Table 2, the replacement of  $^{238}\text{U}$  nuclear data gives little effect on  $k_{inf}$  of the infinite array system. So, it is clear that the difference of inelastic scattering matrix, especially that of the continuum, affects strongly  $k_{eff}$  prediction of experimental cores through the change in neutron leakage from the cores.

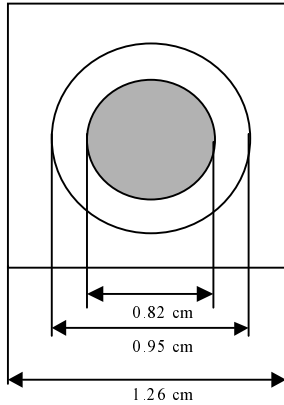


Fig.6 PWR standard cell

Table 2 Effect of  $^{238}\text{U}$  on infinite lattice

		$k_{inf}$
ENDF/B-VI	$^{238}\text{U}$	$1.38273 \pm 0.0153\%$
JENDL-3.2	$^{238}\text{U}$	$1.38254 \pm 0.0153\%$

Secondly, the fission-reaction rate ( $\bar{\nu}_f$ ) averaged  $\nu$ -value of JENDL3.2 in the thermal energy range below 2.1 eV was calculated and then  $\nu$ -value of  $^{235}\text{U}$  of JENDL-3.2 was found to be bigger than that of ENDF/B-VI by 0.14% and the adjustment to  $\nu$ -value of  $^{235}\text{U}$  of ENDF/B-VI increase multiplication factor by 0.09%  $k/k$ .

$$\bar{\nu}_t^{JENDL3.2} = \frac{\int \nu \sigma \phi E}{\int \sigma \phi dE} = 2.4372, \quad \bar{\nu}_t^{ENDF/B-VI} = 2.4338, \quad f = \frac{\bar{\nu}_t^{JENDL3.2}}{\bar{\nu}_t^{ENDF/B-VI}} = 1.0014.$$

Energy dependence of  $^{235}\text{U}$ -values is presented in Fig.7.

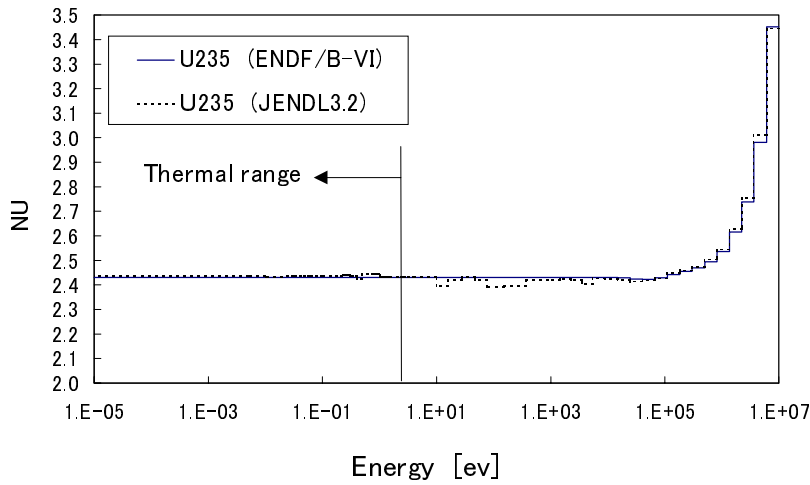


Fig.7 Number of neutrons per fission

The effect of the replacement of  $^{238}\text{U}$  is 0.2% k/k and the adjustment of  $^{235}\text{v}$  is 0.1% k/k. Finally, summing up those effects, we can explain 0.3% difference totally in 0.4 ~ 0.5% difference found in Table 1. It is shown in Fig.2 and Fig.3 that the modified library taken into account of them gives almost the same calculation accuracy of  $k_{\text{eff}}$  for both  $\text{UO}_2$  and MOX cores.

The effect on  $k_{\text{eff}}$  due to the change in  $^{238}\text{U}$  and  $^{235}\text{v}$  data with fuel burnup have been also evaluated with 2-D transport depletion calculation code PHOENIX-P. Nuclear data of both libraries were processed and 70 energy-group libraries were generated with NJOY for this purpose. A  $17 \times 17$  PWR standard assembly was used for the evaluation. The result is shown in Fig.8. It can be found from the figure that the total effect on  $k_{\text{eff}}$  is 0.1% k/k at 0 MWd/t and -0.07% k/k at 60 GWd/t for a PWR  $17 \times 17$  standard assembly with 4.1 w/o enriched  $\text{UO}_2$  rods.

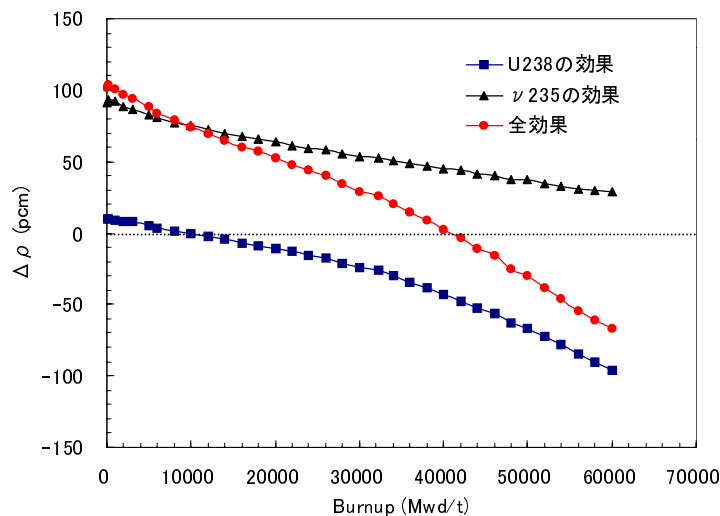


Fig.8 Change in  $k_{\text{eff}}$  with Burnup

The effect of the difference of nuclear data between JENDL-3.2 and ENDF/B-VI on  $k_{\text{eff}}$  value was investigated for the TCA  $15 \times 15$   $\text{UO}_2$  core with fuel rods of 2.6w/o  $^{235}\text{U}$ . The results are shown in the Table 3 where, e.g., in the case of “JENDL-3.2 base”, the reference  $k_{\text{eff}}$  value is based on all the JENDL-3.2 data and the nuclear data of a nuclide is replaced with the corresponding data of ENDF/B-VI. Considering the result obtained previously with regard to  $^{235}\text{U}$ , it can be concluded that the use of the JENDL-3.2 data with  $^{235}\text{U}$  of ENDF/B-VI whose  $^{235}\text{v}$  in thermal range is adjusted to the average value of JENDL-3.2 gives good criticality :  $k_{\text{eff}}=0.99916+0.0009=1.00006$ .

Table 3  $k_{\text{eff}}$  values calculated with MVP for the TCA  $15 \times 15$  core

JENDL3.2 Base			ENDF/B-VI Base		
Cross-section Library	MVP		Cross-section Library	MVP	
	Keff	(%)		Keff	(%)
J3.2 (H,O,Al,U235,U238)	1.00293±0.0236	0.000	ENDF/B-VI (H,O,Al,U235,U238)	0.99487±0.0234	0.000
J3.2 (O,Al,U235,U238) ENDF/B-VI(H)	1.00258±0.0232	-0.035	ENDF/B-VI (O,Al,U235,U238) J3.2 (H)	0.99593±0.0239	0.107
J3.2 (H,Al,U235,U238) ENDF/B-VI(O)	1.00275±0.0239	-0.018	ENDF/B-VI (H,Al,U235,U238) J3.2 (O)	0.99626±0.0248	0.140
J3.2 (H,O,U235,U238) ENDF/B-VI(Al)	1.00172±0.0239	-0.120	ENDF/B-VI (H,O,U235,U238) J3.2 (Al)	0.99607±0.0240	0.121
J3.2 (H,O,Al,U238) ENDF/B-VI(U235)	0.99916±0.0239	-0.376	ENDF/B-VI (H,O,Al,U238) J3.2 (U235)	0.99873±0.0244	0.388
J3.2 (H,O,Al,U235) ENDF/B-VI(U238)	0.99995±0.0238	-0.297	ENDF/B-VI (H,O,Al,U235) J3.2 (U238)	0.99726±0.0243	0.241
ENDF/B-VI(H,O,Al,U235,U238)	0.99487±0.0234	-0.808	J3.2(H,O,Al,U235,U238)	1.00293±0.0236	0.808

H is the cross-section of  $\text{H}_2\text{O}$ .

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**3. Conclusions**  $\text{UO}_2$  and MOX core experiments of TCA have been analyzed with MVP using the libraries based on ENDF/B-VI and JENDL-3.2. It has been found that the replacement of  $^{238}\text{U}$  data with the JENDL-3.2 data and the adjustment of  $^{235}\text{v}$ -value raise the  $k_{\text{eff}}$  values obtained using ENDF/B-VI based library by 0.3% for  $\text{UO}_2$  cores, but still underpredict  $k_{\text{eff}}$  values. On the other hand, the use of a combined library of JENDL-3.2 for H, O, Al,  $^{238}\text{U}$  and ENDF/B-VI for  $^{235}\text{U}$  whose  $^{235}\text{v}$  in thermal energy region is adjusted to the average value of JENDL-3.2 seems to give a good prediction of  $k_{\text{eff}}$ , while the adequacy should be examined from other points of view, e.g., reaction rate ratio measurements, PIE data etc.

#### Acknowledgements

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#### Reference

- [1] Takano, H., et al: “Reactor Benchmark Testing for JENDL3.2, JEF-2.2, and ENDF/B-VI-2,” Int. Conf. Phys. of Nucl. Sci. Technol. (1998) .